

Birds of a Feather Flock Together and Opposites Attract: The Nonlinear Relationship Between Personality and Friendship

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Abstract. Whether birds of a feather flock together or opposites attract is a classical research question in social and personality psychology. In most existing studies, correlation-based techniques are commonly used to study the similarity/dissimilarity among social entities. Social network data comprises two primary components: actors and the possible social relations between them. It, therefore, has observations on both the dyads with and without social relations. Because of the availability of the baseline group (dyads without social relations), it is possible to contrast the two groups of dyads using social network analysis techniques. This study aims to illustrate how to use social network analysis techniques to address psychological research questions. Specifically, we will investigate how the similarity or dissimilarity of actor's characteristics relates to the likelihood for them to build social relations. By analyzing a college friendship network, we found the quadratic relations between personality similarity and friendship. Both very similar and very dissimilar personalities boost friendship among college students.

Keywords: Friendship network · Personality · Social network analysis · Quadratic relation · Factor analysis

1 Introduction

Social relations play a crucial role in an individual's social and behavioral development (Cacioppo & Cacioppo, 2014; House, Landis, & Umberson, 1988; McCamish-Svensson, Samuelsson, Hagberg, Svensson, & Dehlin, 1999; Umberson, Crosnoe, & Reczek, 2010). Close and healthy social relations benefit people's subjective well-being in their life span (McCamish-Svensson et al., 1999; Seeman, 2001; Waldinger, Cohen, Schulz, & Crowell, 2015). Social relations also impact people's health behavior such as alcohol use (Balsa, Homer, French, &

Norton, 2011). Understanding and predicting the formation of social relations is thus of enormous interests to researchers and has been traditionally studied in social and personality psychology (e.g., Bahns, Crandall, Gillath, & Preacher, 2017; Cacioppo & Cacioppo, 2014)

In the existing literature, the principle of homophily is “believed” to be the mainstream of the formation of social relations. In other words, individuals in close social relations share many similar characteristics (McPherson, Smith-Lovin, & Cook, 2001; Rushton & Bons, 2005). A large body of research has investigated the presence of similar personality attributes in close relations such as romantic relations and friendships (e.g., Asendorpf & Wilpers, 1998; Harris & Vazire, 2016; Liu, Jin, & Zhang, 2018; Youyou, Stillwell, Schwartz, & Kosinski, 2017). Much of the research found no or weak personality similarity (Altmann, Sierau, & Roth, 2013; Watson, Beer, & McDade-Montez, 2014; Watson, Hubbard, & Wiese, 2000). Others found moderate similarities in some of the Big Five personality factors (McCrae et al., 2008). Youyou et al. (2017) revealed personality similarity among couples and friends. Another study found that individuals tended to select those with similar personalities as friends (Bahns et al., 2017). Hudson and Fraley (2014) found a quadratic relationship between partners’ personality-trait-similarity and relationship satisfaction among people with low avoidance and high anxiety. The existing conclusions seem to be inconclusive.

There are at least two potential reasons that account for the inconsistency in the literature. In most of these studies, only data on dyads are available due to the data collection methods such as collecting data from friends whereas data on dyads without social relations are not available. Therefore, few of these studies actually contrasted the two types of dyads due to the lack of the baseline group. Moreover, correlation analysis is the dominant approach used in studying the similarities of two actors forming dyads, which only focuses on the linear relationship between two variables and overlooks the potential nonlinear relationships.

Social network data, however, contain both dyads with social relations and dyads without social ties. A social network comprises a group of actors and the potential relationship between them (Wasserman & Faust, 1994). In a network graph \mathbf{M} , nodes represent “actors,” and they could be any entities such as students in a friendship network, research institutions in a collaboration network, and variables in a variable network (Epskamp, Rhemtulla, & Borsboom, 2017). The ties/edges in a network display the relations, interactions or dependence among “actors.” It thus provides a premise to study the association between actor attribute similarity and social relations as in previous studies. It further allows researchers to compare two types of dyads using tools other than correlation analysis. It potentially leads to more interpretable results. In recent years, efforts have been made to address social and psychological research questions from the network perspective. Sweet (2016) reviewed common descriptive methods and network models for educational and psychological research. Clifton and Webster (2017) discussed the use of social network data

to address psychological research questions through several examples. Liu et al. (2018) proposed a structural equation model to predict the existence of binary social relations using the latent personality distance.

The goal of the present work is multifold. First, we introduce some measures to quantify dyads' properties, which are named "nodal/dyadic" covariates. These measures are not necessarily about similarity but could be in any meaningful format. Second, we demonstrate how to use the newly introduced measures to predict social relations using the proposed model by Liu et al. (2018), which provides a primer on predicting social bonds in a network. Third, we illustrate how to conduct the model selection and choose the model that fits the data best.

The rest of this article is structured as follows. First, we describe the college friendship network data collected by the Lab of Big Data at the University of Notre Dame. Next, we explore the factor structures of personality data. We then predict a valued friendship network using student's characteristics and select the model that fits the data best. In the end, we conclude the study with discussions on the current development and future directions.

2 Friendship Network: An Empirical Example

Throughout this paper, we use the data collected by the Lab of Big Data at the University of Notre Dame (Liu et al., 2018).

2.1 Participants

The participants are 162 students in a 4-year college in China. All the students were studying at the school of art and letters while completing the survey. Therefore, the boundary of the friendship network was known before data collection. Among the 162 students, there were 90 female and 72 male students. Their average age was 21.64 years ($SD=0.86$).

2.2 Procedures and Measures

Four types of information are available: (1) friendship networks, (2) actor attributes including demographic information, (3) behaviors, and (4) personalities.

2.2.1 Friendship networks To collect the network data, we gave each student a roster of all the 162 students and asked them to report their acquaintanceship with every other student. The friendship was measured on a 5-point *Likert* scale ranging from "I have never heard about this student." to "The person is one of my best friends." (See Table 1). In the current study, we used the maximal relationship between a pair of students. If two students have different evaluations on the friendship between them, we use the stronger evaluation. Therefore, the relationship is symmetric and non-directional. With

Table 1. 5-point Likert scale for the friendship

Level	Meaning
0	I have never heard the name.
1	I heard about the person but had no personal interaction with her/him.
2	I have met the person a few times but he/she is not a friend of mine.
3	The person is a friend of mine.
4	The person is one of my best friends.

162 students, the network data are recorded in a 162 by 162 matrix \mathbf{M} , which is called a “sociomatrix” in the field of social network analysis. A row of \mathbf{M} contains the responses of the row actor on their friendship relations with the column actors.

A plot of the friendship network with ordinal relations is included in Figure 1. In the heatmap of the friendship network, a darker square represents a stronger relationship between the students in the corresponding row and column. On the diagonal from the bottom left to the upright, there are six blocks standing out with dark color, each containing a group of students with closer relations. Those blocks are clusters of the college student friendship network.

2.2.2 Personality We used the 20-item Mini-IPIP Scale for the Big Five factors of personality (Donnellan, Oswald, Baird, & Lucas, 2006). The five factors measured include Intellect/Imagination (or Openness), Conscientiousness, Extraversion, Agreeableness, and Neuroticism. Each of the five factors is measured by 4 items. Example items of the Mini-IPIP scale are: “In general, I am the life of the party” and “I am not interested in abstract ideas.” The 20 items were rated on a 5-point Likert scale (i.e., 1 = strongly disagree, 2 = somewhat disagree, 3 = neither agree nor disagree, 4 = somewhat agree, and 5 = strongly agree). For reverse coded items, the scores were reversed before analysis.

2.2.3 Actor Attribute Data Participants also reported data on their behaviors. Participants rated themselves on these items using a true or false format. To collect data on the alcohol use, each student reported whether they had drunk alcohol in the past 30 days or not. Among the 162 students, 68 students reported they have drunk alcohol in the past thirty days. Besides, information on academic performance was also available, with scores ranging from 18 to 87. The average academic performance score was 54.99, with a standard deviation of 10.94.

2.3 Overview of Data Analysis

The purpose of the analysis is to exemplify the potentials of social network analysis in psychological research. Specifically, we will investigate how personality predicts friendship. In the literature, there are arguments on both

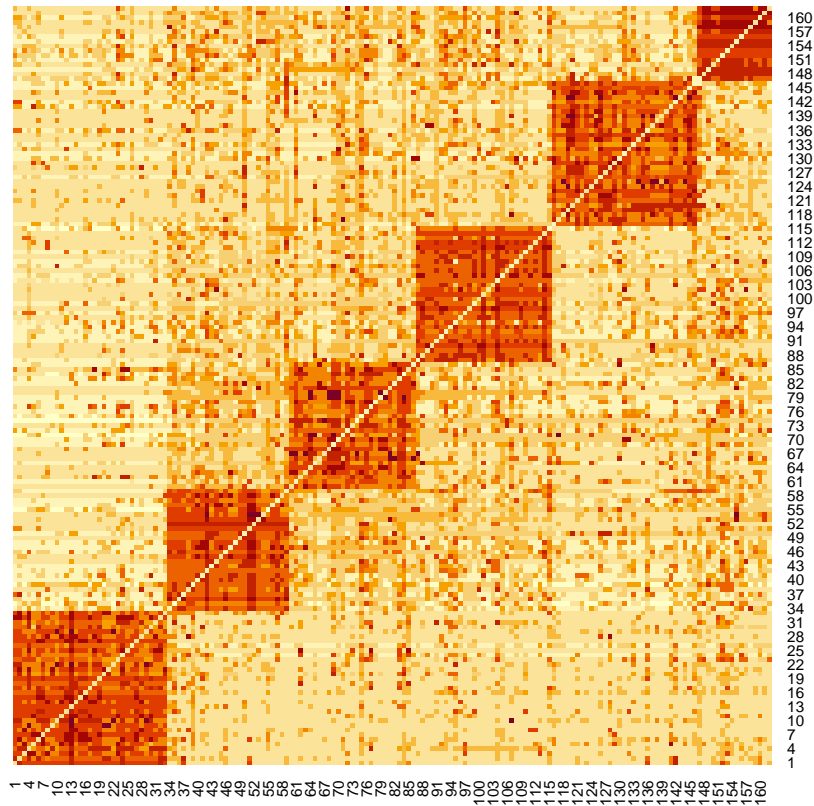


Figure 1. Heatmap of the friendship network. Darker color indicates a higher level friendship

“Birds of a feather flock together,” and “Opposites attract.” If birds of a feather flock together, then we can expect that students with similar personality traits should be more likely to be friends. If opposites attract, then we can expect those with dissimilar personalities should boost the likelihood for them to be friends. If both statements are plausible, then we should expect a nonlinear relation between personality similarity and friendship. In the following, we will first explore the factor structures of personalities.

3 Factor Extraction

We conducted a confirmatory factor analysis (CFA, Cattell, 1952) to evaluate the structure of the latent personality traits. The reliability (α) of the five scales are 0.57 for “intelligence/imagination”, 0.48 for “conscientiousness”, 0.62 for “extraversion”, 0.48 for “agreeableness”, and 0.40 for “neuroticism.” We decided to use two factors—imagination and extraversion—in the CFA because they have relatively high α values. Let $\boldsymbol{\eta}$ be the vector of latent personality factors and \mathbf{w} be their indicators. The CFA model has the following general form,

$$\begin{cases} \mathbf{w}_i &= \mathbf{\Lambda}\boldsymbol{\eta}_i + \boldsymbol{\varepsilon}_i \\ \boldsymbol{\eta}_i &\sim \text{MVN}(\mathbf{0}, \boldsymbol{\Phi}) \\ \boldsymbol{\varepsilon}_i &\sim \text{MVN}(\mathbf{0}, \boldsymbol{\Psi}), \end{cases} \quad (1)$$

where \mathbf{w}_i is the indicator data on actor i , $\boldsymbol{\varepsilon}_i$ is a $J \times 1$ vector of unique factors and it follows a multivariate normal distribution with mean $\mathbf{0}$ and covariance matrix $\boldsymbol{\Psi}$. The factor loading matrix $\mathbf{\Lambda}$ is a $J \times D$ matrix. $\boldsymbol{\Phi}$ is the factor covariance matrix to be estimated. In this model, the unknowns include individuals’ factor scores $\{\boldsymbol{\eta}_i\}_{i=1}^N$ and model parameters $\{\mathbf{\Lambda}, \boldsymbol{\Phi}, \boldsymbol{\Psi}\}$. We fix one factor loading of each factor to be 1 for the purpose of model identification.

We conducted model modification after fitting the model without cross-loadings and correlations among items to explore the factor structure. We ended up with the final model with RMSEA 0.047 and CFI 0.963. The path diagram of the final model is presented in Figure 2.

Recall that the purpose of the current study was to investigate the association between personality similarity and friendships. We, therefore, recorded estimates for both the factor covariance matrix $\boldsymbol{\Phi}$ and individuals’ factor scores $\boldsymbol{\eta}_i$, which will be used to compute the personality similarity (i.e., distance) of any two students. The estimated factor covariance matrix is provided in Table 2. The variance estimates of extraversion and imagination are 0.838 and 0.252, respectively, and their covariance is 0.172.

Table 2. Estimated variance and covariance of latent factors

cov(,)	Extraversion Imagination	
Extraversion	0.838	0.172
Imagination	0.172	0.252

Despite many factor score estimators, the Thurstone-Thomson “regression” factor scores (Thurstone, 1935) were extracted and used in the subsequent analysis following the recommendations by both Devlieger, Mayer, and Rosseel (2016) and Liu et al. (2018). The scatterplot and the histograms of the predicted factor scores are provided in Figure 3. Each dot in Figure 3 represents the location of a student in the personality space formed by the scores of extraversion and imagination. Two students sharing similar personality traits in extraversion and imagination would stay close to each other in the personality space.

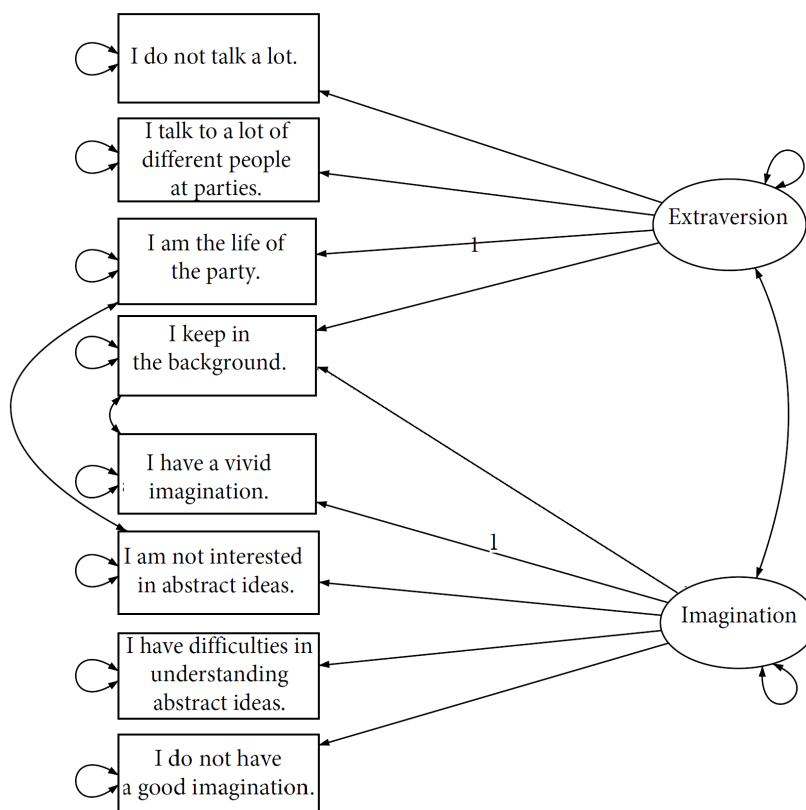


Figure 2. Path diagram of the CFA model of Imagination and Extraversion

4 Probit Model for Ordinal Networks

The model we will introduce is built on the prior work on structural equation modeling of social networks by Liu et al. (2018). In this modeling framework, individuals are assumed to hold a position in a latent space formed by personality traits (i.e., personality space). The distance/(dis)similarity between two individuals in the personality space predicts how likely they connect in the manifest social world. This modeling framework is developed to predict social relations using individuals' characteristics. This model can particularly investigate whether similar personalities or dissimilar personalities boost friendships among college students.

In the following, we will present the model in a form for analyzing networks with ordinal relations and demonstrate its applications in examining the relationship between personality similarity and friendships. We will compare the following plausible hypotheses: (1) similar personality traits promote friendship;

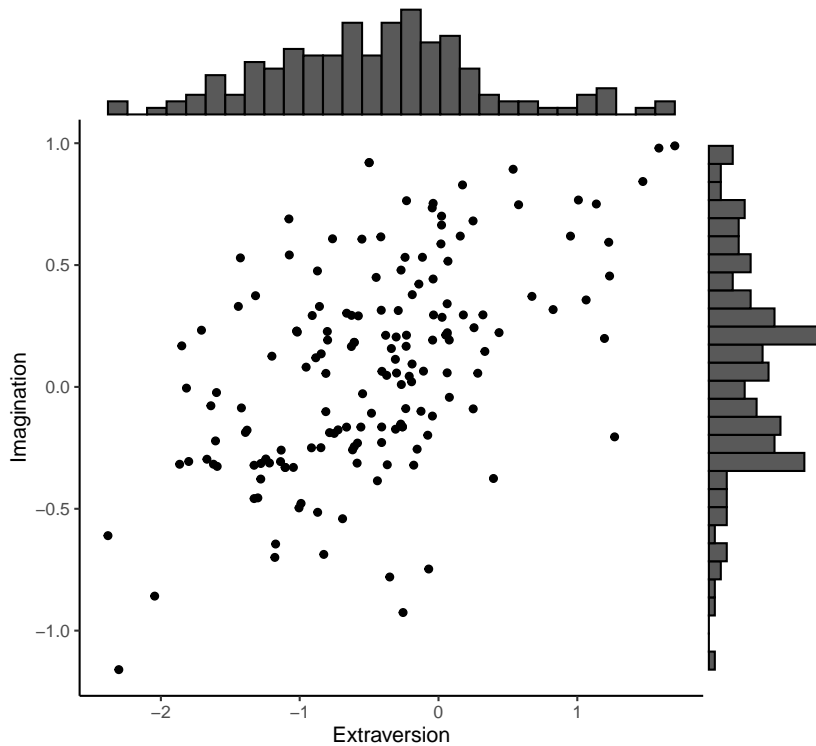


Figure 3. Predicted factor score

(2) dissimilar personality traits imply a higher chance to be friends; or (3) both are plausible.

The data analysis will use a three-phase procedure. First, we will define “nodal covariates” (i.e., dyads level covariates) based on the research hypotheses of interests. Second, we will build a Probit model to investigate how the nodal covariates predict friendship. Third, we will conduct likelihood ratio tests to select the model with the best fit for the data.

4.1 Nodal Covariates

The study focuses on predicting the ordinal ties in the friendship network, which is a dyadic level analysis of social networks. Therefore, we need to construct dyadic covariates describing the characteristics of a pair of students. In addition to personality traits, we also consider three manifest covariates—gender, academic performance, and class membership.

Same-gender friendship has been of interest to researchers (Benenson, 1990; Elkins & Peterson, 1993; Jones, 1991; Zarbatany, Conley, & Pepper, 2004). To

test the effect of gender on friendship, we define the following nodal covariate,

$$h_{\text{gender}}(i, j) = \begin{cases} 1 & \text{if students } i \text{ and } j \text{ are of the same gender} \\ 0 & \text{otherwise.} \end{cases}$$

Using the nodal covariate h_{gender} , we can study the homogeneous gender effect on the acquaintance levels.

Academic achievement is measured using a continuous scale. To quantify the similarity in academic achievement, we define a nodal covariate of academic achievement as the absolute difference of two students' scores

$$h_{\text{score}}(i, j) = |\text{score}_i - \text{score}_j|.$$

The larger value on $h_{\text{score}}(i, j)$, the more discrepancy of students i and j on their academic achievement.

The 162 students participating in our study belonged to different “classes.” Students from the same class take the same courses more often, and potentially have more chances to build friendships. Therefore, we control the class membership effect in our analysis. The nodal covariate of class membership takes value one if two students are from the same class and 0 otherwise. That is

$$h_{\text{class}}(i, j) = \begin{cases} 1 & \text{if students } i \text{ and } j \text{ are from the same class,} \\ 0 & \text{otherwise.} \end{cases}$$

In addition to the three manifest nodal covariates h_{gender} , h_{score} , and h_{class} , we focus on the relationship between the personality similarity and friendships. To quantify the personality similarity, we use the Mahalanobis distance (Mahalanobis, 1936) of the personality factor scores of two students,

$$d_{ij} = h_{\text{personality}}(i, j) = \sqrt{(\boldsymbol{\eta}_i - \boldsymbol{\eta}_j)^t \boldsymbol{\Phi}^{-1} (\boldsymbol{\eta}_i - \boldsymbol{\eta}_j)}, \quad (2)$$

where $\boldsymbol{\eta}_i$ and $\boldsymbol{\eta}_j$ are the vectors of personality factor scores of students i and j , and $\boldsymbol{\Phi}$ is the covariance matrix of personality latent factors. The Mahalanobis distance is the standardized distance of two correlated vectors penalized by the covariance between them.

We want to note that the concept of the “nodal” covariate is flexible to include any statistics that summarize the information of dyads. Researchers can define their nodal covariates based on their research hypothesis. Moreover, a nodal covariate is not necessarily capturing the similarity of actors as exemplified. Instead, it could be of any type. To provide an example, one can define overall academic achievement as the sum of scores of two students and test whether the overall score relates to the friendship or not. Instead of studying the effect of similar personality, one could also study the overall extraversion level of two students and investigate its impact on the friendship between the two students.

4.2 Probit Regression Analysis of Ordinal Networks

To model the association between personality similarity and friendship, we extended the work by Liu et al. (2018) to undirected valued networks with ordinal relations. A probit model is adopted to predict the ordinal relations using nodal covariates (Agresti, 2013). Let m_{ij} be the level of friendship between student i and j . It could take one of the five ordinal values 0, 1, 2, 3, or 4 in the college friendship introduced in the previous section. A greater value indicates a stronger relationship between the two students. For a level $k = 0, 1, 2, \dots, 4$, let $\pi_{ij}^{(k)}$ be the probability for m_{ij} to be in the k 'th category,

$$p(m_{ij} = k) = \pi_{ij}^{(k)}, \quad \text{for } k = 0, 1, \dots, 4. \quad (3)$$

The cumulative probability for a tie in a category k and below is

$$p(m_{ij} \leq k) = \pi_{ij}^{(0)} + \pi_{ij}^{(1)} + \dots + \pi_{ij}^{(k)}, \quad \text{for } k = 0, 1, 2, \dots, 4 \quad (4)$$

and $\sum_{k=0}^4 \pi_{ij}^{(k)} = 1$, since any friendship tie must fall in one of the five categories. To predict the probability for a tie to fall in a category using nodal statistics on dyads, we use an ordered probit model,

$$\begin{cases} \text{Probit } [p(m_{ij} \leq k)] &= F^{-1}[p(m_{ij} \leq k)] & \text{for } k = 0, 1, \dots, 3 \\ &= \tau_{k|k+1} - (\boldsymbol{\beta}'\mathbf{h}_{ij} + \gamma d_{ij}) \\ \pi_{ij}^{(4)} &= 1 - \sum_{k=0}^3 \pi_{ij}^{(k)} \end{cases} \quad (5)$$

where $F(\cdot)$ is the cumulative density function (CDF) of the standard normal distribution (i.e., $N(0, 1)$), and d is the latent personality distance computed as $d = \sqrt{(\boldsymbol{\eta}_i - \boldsymbol{\eta}_j)' \boldsymbol{\Phi}^{-1}(\boldsymbol{\eta}_i - \boldsymbol{\eta}_j)}$ as in Equation (2). The parameters $\boldsymbol{\beta}$ and γ are coefficients of manifest nodal covariates and latent factor distance (i.e., d). Because $F^{-1}(\cdot)$ is an increasing function, the intercept coefficients must follow an ordered sequence,

$$\tau_{0|1} \leq \tau_{1|2} \leq \dots \leq \tau_{3|4}.$$

To further understand the impact of the slope parameter γ on the propensities of categories, four plots with different values for γ are provided in Figure 4. We generate data from a model with four categories, and the three thresholds are $\tau_{0|1} = -1$, $\tau_{1|2} = 0$, and $\tau_{2|3} = 1$ and one manifest covariate (i.e., $h1$) whose coefficient $\beta = 0.6$. Given $h1 = 0$, we computed the implied cumulative probabilities with varying d . In Figure 4, the red, green, blue, and purple curves are the probability for a tie in category 0, category 0 or 1, category 0, 1, or 2, and category 0, 1, 2, or 3.

First, when $\gamma < 0$ (Plot (a) and (b) in Figure 4), the cumulative probabilities are increasing as the latent distance d increases. Thus, the probability for a tie in a higher-level category decreases. When $\gamma > 0$ (Plot (c) and (d)), the trajectories of the cumulative probability are in the opposite direction. A positive value of γ indicates that with a larger latent distance d , the probability for a relationship to be in a higher-level category increases. The magnitude of γ (i.e., $|\gamma|$) tells the

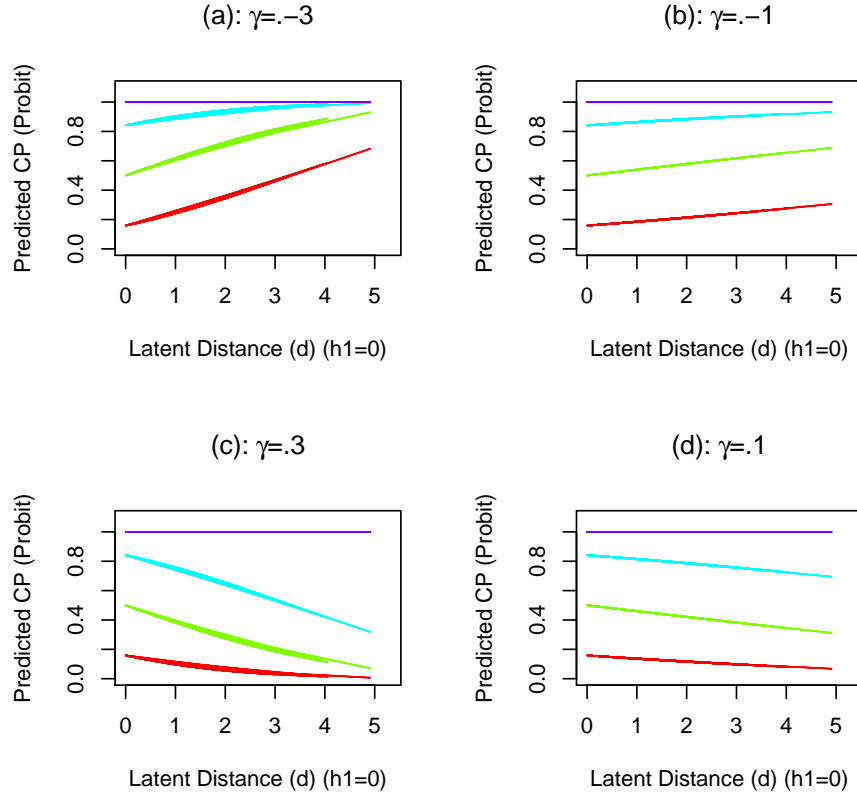


Figure 4. Plots of cumulative probabilities (CP) with different slope parameters in a model with 4 ordinal levels given the level of other covariates. The red, green, blue, and purple curves are the CP up to category 0, 1, 2, and 3.

extent to which the latent distance affects the cumulative probability. A larger $|\gamma|$ implies stronger impacts of latent distance d on the friendship.

To investigate the potential higher-order relationship between the personality similarity and friendship, we fit the model with the quadratic term of personality distance. To check whether the quadratic model is the conclusive model, we can fit the model with the cubic term of the personality distance. Therefore, we fit three competing models: a linear model with the first-order distance, i.e., d_{ij} as a predictor, a quadratic model with d_{ij}^2 as a predictor, and a cubic model with d_{ij}^3 as a predictor.

4.2.1 Linear Probit Model In the linear probit model, we include three manifest nodal covariates h_{gender} , h_{score} , and h_{class} as well as the latent

personality distance d ,

$$\begin{cases} P(m_{ij} \leq k) & = \pi_{ij}^0 + \pi_{ij}^1 + \cdots + \pi_{ij}^{(k)}, & \text{for } k = 0, 1, \dots, 4. \\ \text{Probit } [P(m_{ij} \leq k)] & = F^{-1}[P(m_{ij} \leq k)] & \text{for } k = 0, 1, \dots, 3 \\ & = \tau_{k|k+1} - (\beta_1 h_{gender}(i, j) + \beta_2 h_{score}(i, j) & (6) \\ & \quad + \beta_3 h_{class}(i, j) + \gamma d_{ij}) \\ \pi_{ij}^{(4)} & = 1 - \sum_{k=0}^3 \pi_{ij}^{(k)} \end{cases}$$

In this model, the coefficient γ explains the extent to which the personality distance d_{ij} predicts friendship. With a negative γ , the probability of having a higher level of friendship is greater when d_{ij} is smaller, so the more similar personalities associate with a higher chance to have a closer friendship. If γ is positive, then dissimilar personalities boost friendship.

4.2.2 Quadratic Probit Model In the second model, we also include a quadratic term of the latent personality distance, and the model becomes,

$$\begin{aligned} \text{Probit } [P(m_{ij} \leq k)] &= F^{-1}[P(m_{ij} \leq k)] && \text{for } k = 0, 1, \dots, 3 \\ &= \tau_{k|k+1} - (\beta_1 h_{gender}(i, j) + \beta_2 h_{score}(i, j) + \beta_3 h_{class}(i, j) && (7) \\ &\quad + \gamma_1 d_{ij} + \gamma_2 d_{ij}^2). \end{aligned}$$

This model is useful for investigating the potential quadratic relationship between the personality similarity and friendship, and it also helps identify the transition points of the trend.

4.2.3 Cubic Probit Model The cubic model includes the third-order of the distance, i.e., d_{ij}^3 , in the analysis,

$$\begin{aligned} \text{Probit } [P(m_{ij} \leq k)] &= F^{-1}[P(m_{ij} \leq k)] && \text{for } k = 0, 1, \dots, 3 \\ &= \tau_{k|k+1} - (\beta_1 h_{gender}(i, j) + \beta_2 h_{score}(i, j) + \beta_3 h_{class}(i, j) && (8) \\ &\quad + \gamma_1 d_{ij} + \gamma_2 d_{ij}^2 + \gamma_3 d_{ij}^3) \end{aligned}$$

By fitting the cubic model, we can investigate if there is more than one transition point for the relationship between personality similarity and friendship.

To estimate the model, we first evaluate the factor structure of the extroversion and imagination, and obtain the model parameter estimates and the Thurstone-Thomson “regression” factor scores $\hat{\boldsymbol{\eta}}_i$ and $\hat{\boldsymbol{\eta}}_j$ as discussed in the previous section. We then compute the estimated personality distance

$$\hat{d}_{ij} = \sqrt{(\hat{\boldsymbol{\eta}}_i - \hat{\boldsymbol{\eta}}_j)^t \hat{\boldsymbol{\Phi}}^{-1} (\hat{\boldsymbol{\eta}}_i - \hat{\boldsymbol{\eta}}_j)}.$$

According to the suggestions by Liu et al. (2018), the use of Thurstone-Thomson factor scores led to asymptotically unbiased estimates for the γ parameter.

5 Result

In this section, we will present the results of the three models discussed in the previous section

5.1 Model Selection

To evaluate the relative performance of the three models (i.e., linear, quadratic, and cubic probit model), we conducted likelihood ratio tests using the saved deviance in Table 3. For the linear model against the quadratic model, the Chi-square statistic is 9.514 and with a p-value of .002. Hence, the quadratic model is significantly better than the linear model. When the quadratic model is compared against the cubic (third-order) model, the Chi-square statistic is 0.318 with a p-value of .573. Thus, the cubic model is not significantly better than the quadratic model. The quadratic model is thus the best model.

Table 3. Likelihood ratio test of the three nested models

Model	Deviance	Test	Df	LR Stat	Pr(Chi)
1 Linear	28560.55				
2 Quadratic	28551.03	1 vs 2	1	9.514	.002
3 Cubic	28550.71	2 vs 3	1	0.318	.573

5.2 Model Parameter Estimates

Because the quadratic model fits the data best, we would interpret the relationship between the personality similarity and friendship using the estimates of the quadratic model, which are provided in Table 4.

Table 4. Parameter estimates of the quadratic model

Par	Est	Std.Error	t.value	p-value
β_{gender}	0.549	0.02	26.839	< .001
β_{score}	-0.111	0.013	-8.773	< .001
β_{class}	2.439	0.032	75.549	< .001
γ_1	-0.098	0.044	-2.238	.025
γ_2	0.038	0.012	3.088	.004
τ_0	0.228	0.04	5.694	< .001
τ_1	1.113	0.041	27.214	< .001
τ_2	1.720	0.043	40.097	< .001
τ_3	2.888	0.049	58.565	< .001
Residual deviance			228551.03	

By plugging the model parameter estimates into the quadratic model (Equation 7), we obtained the predicted cumulative probability for a tie to be in a category k ($k=0,1,2$ or 3) or below¹. Equivalently, we can also get the probability for a tie to be in a category above k ($k = 0, 1, 2,$ or 3)² and we will use them for the interpretation in the following.

First, all parameters are statistically significant, based on the significance level of 0.05. The coefficient of h_{gender} is 0.549. Given the levels for other covariates and latent personality distance being the same, two students of the same gender tend to have a closer relationship than otherwise, and they are less likely to have a lower-level friendship. Therefore, gender homogeneity boosts a higher level of acquaintanceship. *Second*, the coefficient h_{score} has a point estimate -0.111 (p-value < 0.001). Given the same levels of other covariates and latent distance, students with more similar academic achievement (i.e., h_{score} is small) have a higher level of friendship with a greater probability than two students with some very different academic achievements. *Third*, the coefficient estimate of h_{class} is 2.439. Thus, two students from the same class are more likely to have a closer relationship. For instance, $\pi^{(4)}$ is larger for two students from the same class.

The coefficient estimate of the first-order distance (i.e., γ_1) is -0.098 (p-value = 0.025) and that of the second-order distance is 0.038 (p-value = .004). For $k = 0, 1, 2,$ or 3 , the quantity $\pi^{(k+1)} + \dots + \pi^{(4)}$ is the probability for a tie to fall in a category above k . To better understand the relationship between personality similarity and friendship, we plotted these probabilities against the latent personality distance d , given two students are of the same gender (i.e., $h_{gender} = 1$), have the same academic score (i.e., $h_{score} = 0$), and are from the same class (i.e., $h_{class} = 1$). These plots are provided in Figure 5.

¹ The predicted cumulative probability is computed as

$$\begin{aligned} p(m \in 0) &= F(0.228 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 0, 1) &= F(1.113 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 0, 1, 2) &= F(1.720 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 0, 1, 2, 3) &= F(2.888 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2). \end{aligned}$$

² The probability for a tie to be in a category above k ($k = 0, 1, 2,$ or 3)

$$\begin{aligned} p(m \in 1, 2, 3, 4) &= 1 - F(0.228 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 2, 3, 4) &= 1 - F(1.113 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 3, 4) &= 1 - F(1.720 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2) \\ p(m \in 4) &= 1 - F(2.888 - 0.549h_{gender} + 0.111h_{score} - 2.439h_{class} + 0.098d - 0.038d^2). \end{aligned}$$

For a level $k = 0, 1, 2,$ or 3 , the probability for tie to have a level above k is analogous to the probability of being “1” if we dichotomize the ordinal relations into binary relations at the level k .

All four probability curves are U-shapes. They decrease first and increase afterward when the latent distance increases. They reach their minimum values when the latent personality distance between the two students is 1.289. When the latent distance approaches 0, the probability for a tie in a category above k (for $k = 0, 1, 2,$ or 3) becomes larger, which indicates that the propensity for two students to have a higher level of acquaintanceship increases. Thus, similar personalities in extraversion and imagination are beneficial to the friendship between two students. When the latent personality distance is greater than 1.289, the probability for a friendship to be in a category above k increases with a larger latent personality distance. Thus, dissimilar personalities in extraversion and imagination also contribute to friendship. The results from this empirical study clearly support both “Birds of a feather flock together,” and “Opposites attract.”

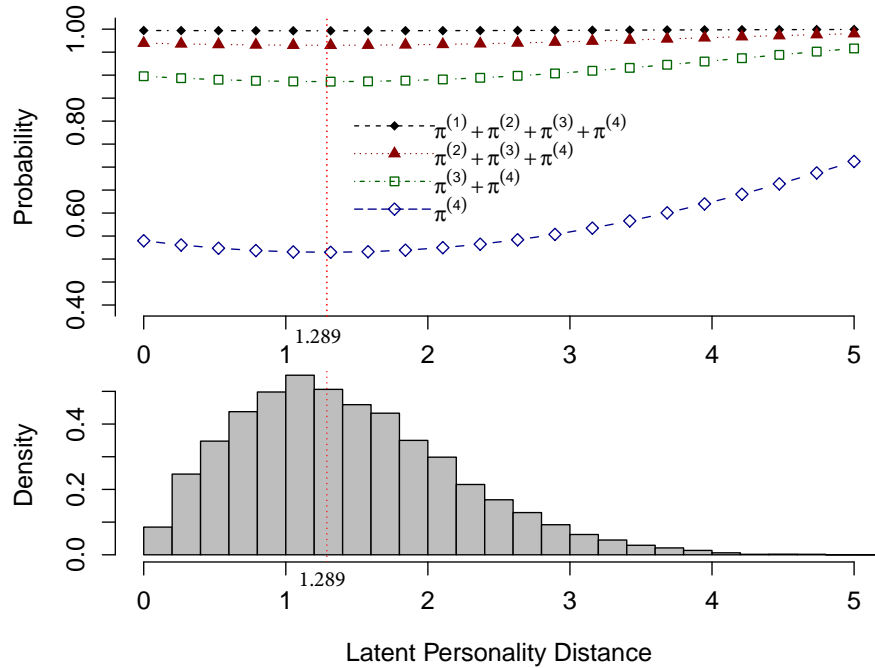


Figure 5. The top plots are the cumulative probabilities of predicted categories varying with respect to latent personality distances, and the four curves from bottom to top are the probability for a tie to be in level 4, level 3 or 4, level 2, 3, or 4, and level 1, 2, 3, or 4. The bottom panel is the density plot of personality distances; the vertical red line lies at $d = 1.289$.

6 Discussion and Conclusion

Social network analysis has been increasingly popular in recent decades. Network data are now easy to collect than ever due to the development of computer techniques. A social network comprises two primary elements: actors and potential social ties. There are observations on both dyads with social relations and dyads without social relations in social network data. Therefore, it allows researchers to understand what and how actors' characteristics predict social relations by contrasting these two groups of dyads. In the current study, we illustrated how to predict social relations using actors' characteristics by analyzing a college friendship network.

To analyze the ordinal/valued friendship network, we extended the work by Liu et al. (2018), which was built to analyze social networks with binary relations. A probit regression model was used to predict the ordinal social ties using the information of dyads. Specifically, we studied how gender homogeneity, similar academic achievements, class membership, and similar personalities predicted college student's friendship. To investigate the potential quadratic relationship between personality similarity and friendship, we fitted three competing models: a linear model with only the linear term of latent distance (i.e., d), a quadratic model with both a linear term and a quadratic term of the latent personality distance (i.e., both d and d^2), and a cubic model with also the third order of the latent personality distance. The quadratic model was significantly better than the linear model but not statistically different from the cubic model. Therefore, the quadratic models won both the linear and cubic models.

Based on the results of the quadratic model, students of the same gender or from the same class were more likely to have closer friendships. Students with similar academic scores were more likely to have higher levels of acquaintanceship. The association between personalities and friendship was mixing. Two students tended to have closer friendship relations if they had very similar personalities in extroversion and imagination. At the same time, if they were very dissimilar in those two personality traits, their friendship was more likely to fall in a higher level category. Hence, "Both birds of a feather flock together" and "Opposites attract" are possible.

Although we fitted the model for undirected networks, the modeling framework could be extended for networks with directed relations. Based on the heatmap (Figure 1), there are several communities/clusters in the college friendship network. In a cluster, students share some common characteristics. In the future, we would also like to fit multilevel models for the potential heterogeneity in the relationship between personality and friendship.

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